### Unsupervised vs. Supervised Learning

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Unsupervised vs. Supervised Learning

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- What Is Machine Learning?
- 2 Supervised Learning: Classification
- Onsupervised Learning: Clustering
- 4 Supervised: K Nearest Neighbors Algorithm
- 5 Unsupervised: K-Means

• **Modeling: model** - specification of a mathematical (or probabilistic) relationship that exists between different variables.

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- Machine Learning creating and using models that are learned from data (predictive modeling or data mining)

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Examples in NLP:

???

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### Examples in NLP:

- Speech Recognition
- Language Identification
- Machine Translation
- Document Summarization
- Question Answering
- Sentiment Detection
- Text Classification

#### supervised: data labeled with the correct answers to learn from



### Approaches

unsupervised: no label given, purely based on the given raw data  $\Rightarrow$  find common structure in data



### Unsupervised Learning: General Examples

• you see a group of people: divide them into groups

# Unsupervised Learning: General Examples



• cluster city names, trees

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- cluster similar blog posts: understand what the users are blogging about.

• predict how I'm going to vote!

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- better idea???

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- $\bullet\,$  new approach look at those neighbors with similar features  $\rightarrow\,$  better prediction!

• classify a new object

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- classify a new object
- find the object in the training set that is most similar
- assign the category of this nearest neighbor

## K Nearest Neighbor (KNN) Classification

Take k closest neighbors instead of one



## K Nearest Neighbor (KNN) Classification

k = 5; 10



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# K Nearest Neighbor (KNN) Classification: Data points

• Data points are vectors in some finite-dimensional space.

# K Nearest Neighbor (KNN) Classification: Data points

- Data points are vectors in some finite-dimensional space.
- '+' and '-' objects are 2-dimensional (2-d) vectors:



• if you have the **heights**, **weights**, and **ages** of a large number of people, treat your data as 3-dimensional vectors (height, weight, age):

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#### How we can represent a document???

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• fixed set of elements (e.g., documents):  $D = \{d_1, ..., d_n\}$ 

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- feature weights are numerical statistics (TF-IDF)

### Document Representation: binary

Vectorize a text corpus, by turning each text into a vector where the coefficient for each token could be **binary**:

```
tokenizer.fit_on_texts(X_train)
tokenizer.word_index
>>>{'first': 2, 'second': 4, 'sentence': 3,
      'text': 1, 'third': 5}
```

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### Document Representation: count

Vectorize a text corpus, by turning each text into a vector where the coefficient for each token could based on **word count**:

```
tokenizer.fit_on_texts(X_train)
tokenizer.word_index
>>>{'first': 2, 'second': 4, 'sentence': 3,
    'text': 1, 'third': 5}
```

```
tokenizer.texts_to_matrix(X_train, mode='count')
>>array([[0., 1., 2., 1., 0., 0.],
        [0., 1., 0., 0., 1., 0.],
        [0., 1., 0., 0., 0., 1.]])
```

### Document Representation: tf-idf

Vectorize a text corpus, by turning each text into a vector where the coefficient for each token could based on **tf-idf**:

```
tokenizer.fit_on_texts(X_train)
tokenizer.word_index
>>>{'first': 2, 'second': 4, 'sentence': 3,
    'text': 1, 'third': 5}
```

```
tokenizer.texts_to_matrix(X_train, mode='tfidf')
>>[[0 0.55961579 1.55141507 0.91629073 0 0]
[0 0.55961579 0 0 0.91629073 0]
[0 0.55961579 0 0 0 0.91629073]]
```

def knn\_classify(k, labeled\_points, new\_point):
 """each labeled point is a pair (point, label)"""

# find the labels for the k closest
k\_nearest\_labels = [label for \_,label
in similarities[:k]]

# and choose one
return choose\_one(k\_nearest\_labels)

### Recall: Sort List of Tuples

```
>>> sorted(students)
[('dave', 25), ('jane', 20), ('john',22)]
```

```
>>> sorted(students, key=lambda x: x[1])
[('jane', 20), ('john', 22), ('dave', 25)]
```

>>> **sorted**(students, key=**lambda** x: x[1], reverse=True) [('dave', 25), ('john', 22), ('jane', 20)]

>>> sorted(students, key=lambda x: -x[1]) [('dave', 25), ('john', 22), ('jane', 20)]

```
cosin_sim([1,2],[3,4])
>>> 0.9838699100999074
```

• dot product expresses how much the two vectors are pointing in the same direction

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- if two documents share a lot of common terms, their tf-idf vectors will point in a similar direction

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- if two documents share a lot of common terms, their tf-idf vectors will point in a similar direction
- cosine similarity = an indicator how close the documents are in the semantics of their content

#### What if we have two winners (k = 2)?



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#### Strategies:

Pick one of the winners at random

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What if we have two winners (k = 2)?



Strategies:

- Pick one of the winners at random
- Reduce k until we find a unique winner

### 

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Reduce k until we find a unique winner:

 $reduced_labels = ???$ 

Reduce k until we find a unique winner

 $reduced_labels = labels[:-1]$ 

print(reduced\_labels)

>>> ['sport', 'cars', 'religion', 'religion']

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Reduce k until we find a unique winner

 $reduced_labels = labels[:-1]$ 

print (reduced\_labels)

>>> ['sport', 'cars', 'religion', 'religion']

now 1 winner: 'religion'

# #labels sorted from nearest to farthest labels = ['sport', 'cars', 'religion', 'politics']

#### Winner???

### labels = ['sport', 'cars', 'religion', 'politics']

Winner:	
sport'	]

### labels = ['sport', 'cars', 'cars', 'sport']

#### Winner???

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### labels = ['sport', 'cars', 'cars', 'sport']

Winner:	
'cars'	

**def** choose\_one(labels): """labels are ordered from nearest to farthest"""

counts = Counter(labels)
winner, winner\_count = counts.most\_common(1)[0]

# count number of winners in a list , # i.e. how many words with equal winner\_count? ...

*#if unique winner, so return it* ....

```
#else: reduce the list and try again,
# i.e call choose_one again but with reduced list
```

. . .

```
from collections import Counter
colors = ['red', 'blue', 'red', 'green',
                    'blue', 'blue', 'red']
cnt = Counter(colors)
print(cnt)
>>> Counter({'red': 3, 'blue': 3, 'green': 1})
```

```
most_common_tuple = cnt.most_common(1)
print(most_common_tuple)
>>>[('red', 3)]
```

```
winner, winner_count = most_common_tuple[0]
print(winner, winner_count)
>>> red 3
```
- fixed set of elements (e.g., documents):  $D = \{d_1, ...d_n\}$
- document d (data point) is represented by a vector of features:  $d \in \mathbb{N}^k \rightarrow d = [x_1 x_2 ... x_k]$
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- weights are not re-weighted during learning  $\rightarrow$  KNN is "non-parametric" classifier

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- **Goal** find the most similar document for a given document *d* and assign the same category (1NN classification)

• clustering algorithm

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- the number of clusters k is chosen in advance

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- the number of clusters k is chosen in advance
- partition the inputs into sets  $S_1, ..., S_k$  using cluster centroids

#### K-means clustering technique



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k-means clustering technique

- In andomly initialize cluster centroids
- assign each point to the centroid to which it is closest:
  - use Euclidean distance to measure the distance

$$d(p,q) = \sqrt{\sum_{i=1}^{n} (q_i - p_i)^2}$$
(1)

- recompute cluster centroids
- go back to 2 until nothing changes (or it takes too long)

```
class KMeans:
    """ performs k-means clustering"""
```

```
def __init__(self, k):
    self.k = k # number of clusters
    self.means = None # means of clusters
```

```
def classify(self, input):
    """ return the index of the cluster
    closest to the input (step 2)"""
    return min(range(self.k),
        key=lambda i:
        distance(input, self.means[i]))
```

# Python min() Function

>>> a = [(0.2222, 1), (0.1111, 2), (0.6666, 3)]>>> min(a, key= lambda x: x[0]) >>>(0.1111, 2)

>>> min(a, key= lambda x: x[1]) (0.2222, 1)

>>> **range**(k\_clusters) [0,1,2]

# K-Means

```
def train(self, inputs):
   # choose k random points as the initial means
    self.means = random.sample(inputs, self.k)#step 1
    assignments = None
    while True:
       # Find new assignments
        new_assignments = map(self.classify, inputs)
        if assignments == new_assignments:
            return # If nothing changed, we're done.
        assignments = new_assignments
        for i in range(self.k): #compute new means
            i_points = [p for p, a in zip(inputs,
                       assignments) if a == i]
            if i_points:
                self.means[i] = mean(i_points)
```

```
r = map(func, seq)
```

```
import functools
def fahrenheit(T):
    return ((9.0/5)*T + 32)
temp = [36.5, 37, 37.5, 39]
F = map(fahrenheit, temp)
```

print(list(F))
>>> [97.7, 98.600000000001, 99.5, 102.2]

• organize meetup for users

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organize meetup for users

• goal - choose 3 meetup locations convenient for all users

```
clusterer = KMeans(3)
clusterer.train(inputs)
print(clusterer.means)
```

- organize meetup for users
- goal choose 3 meetup locations convenient for all users

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clusterer.train(inputs)
print(clusterer.means)
```

• you find three clusters and you look for meetup venues near those locations

# Kmeans with NLTK

```
from nltk import cluster
from nltk.cluster import euclidean_distance
from numpy import array
vectors = [array(f) for f in [[3, 3], [1, 2], [4, 2],
                         [4, 0], [2, 3], [3, 1]]
clusterer = cluster.KMeansClusterer(2,
                 euclidean_distance)
clusters = clusterer.cluster(vectors, True)
print('Clustered:', vectors)
print('As:', clusters)
print('Means:', clusterer.means())
>>> Clustered : [array ([3,3]), array ([1,2]),
array ([4,2]), array ([4,0]), array ([2,3]), array ([3,1])]
>>> As: [0, 0, 0, 1, 0, 1]
>>> Means: [array([ 2.5, 2.5]), array([ 3.5, 0.5])]
```

```
# classify a new vector
vector = array([3, 3])
print('classify(%s):' % vector)
print(clusterer.classify(vector))
>>> classify([3 3]):
>>> 0
```

#### Problems

- How many clusters to use?
- How to initialize cluster centroids?

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- $\bullet \rightarrow \textbf{unsupervised}:$  points have no external classification

#### • K-nearest neighbors is a clustering or classification algorithm?

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  - supervised or unsupervised?
  - **supervised:** classifies a point based on the known classification of other points.

### Exercise: Euclidean Distance



distance between person 1 and 2, 1 and 3, 2 and 3?

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(2)

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2

Var1 Var2

20 80

30 44

90 40

Compute the mean vector of given vectors:

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Represent the list of documents in binary mode

```
documents =["test_document1",
    "test_document2",
    "test_document3"]
tokenizer = Tokenizer()
tokenizer.fit_on_texts(X_train)
tokenizer.word_index
>>>{'document1': 2, 'document2': 3,
    'document3': 4, 'test': 1}
doc_matrix = ???
```

#### What is the main difference between supervised and unsupervised learning?

## Exercise: KNN Classifier



- k = 3, the green point = ???
- k = 5, the green point = ???

#### Joel Grus (2015).

#### Data Science from Scratch.

OReilly.

http://choonsiong.com/public/books/Big%20Data/Data%20Science%20from%
20Scratch.pdf

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Foundations of Statistical Natural Language Processing

The MIT Press Cambridge, Massachusetts London, England. http://ics.upjs.sk/~pero/web/documents/pillar/Manning\_Schuetze\_ StatisticalNLP.pdf